

| <b>Semester: VI</b>   |  |         |                     |   |                   |
|---|--|---------|---------------------|---|-------------------|
| <b>MATHEMATICAL MODELING</b>                                    |  |         |                     |   |                   |
| <b>(Theory)</b>   |  |         |                     |   |                   |
| <b>(Group E: Global Elective)</b>                               |  |         |                     |   |                   |
| <b>Course Code</b>  | :  | 18G6E16 | <b>CIE</b>          | : | <b>100 Marks</b>  |
| <b>Credits: L:T:P</b>   | :  | 3:0:0   | <b>SEE</b>          | : | <b>100 Marks</b>  |
| <b>Total Hours</b>  | :  | 39L     | <b>SEE Duration</b> | : | <b>3.00 Hours</b> |
| <b>Course Learning Objectives:</b> The students will be able to |  |         |                     |   |                   |
| <b>1</b>  | Adequate exposure to understand the basic knowledge of mathematical modeling.                                |         |                     |   |                   |
| <b>2</b>  | Use the concepts of discrete process models arising in various fields.                                       |         |                     |   |                   |
| <b>3</b>  | Apply the concepts of modeling of nano liquids which have great significance in engineering practice.        |         |                     |   |                   |
| <b>4</b>  | Demonstrate the practical importance of graph theoretic models, variational problem and dynamic programming. |         |                     |   |                   |

| <b>Unit-I</b>  |  | <b>07 Hrs</b> |
|--|--|---------------|
| <b>Elementary Mathematical Modeling:</b>   |  |               |
| Basic concepts. Real world problems, (Science and Engineering), Approximation of the problem, Steps involved in modeling. Linear growth and decay model, Logistic model, Model of mass-spring-dashpot (present in shock absorbed, mechanical engineering problems), Chemical reaction, Drug absorption from blood stream. Motion of a projectile, Current flow in electrical circuits (LCR). |  |               |
| <b>Unit – II</b>   |  | <b>07 Hrs</b> |
| <b>Discrete Process Models:</b>  |  |               |
| Introduction to Difference equations, Introduction to discrete models-simple examples, Mathematical modeling through difference equations in economics, finance, population dynamics and genetics and probability theory.  |  |               |
| <b>Unit –III</b>   |  | <b>08 Hrs</b> |
| <b>Modeling of Nano Liquids:</b>   |  |               |
| Nano liquids-Basic concepts, Mathematical modeling of nano liquids-Buongiorno Model (Two phase model): Relative importance of the nanoparticle transport mechanisms. Conservation equation for two phase nano liquids: The Continuity equation, Momentum equation and Energy equation.   |  |               |
| <b>Unit –IV</b>  |  | <b>08 Hrs</b> |
| <b>Graph Theoretic Models:</b>   |  |               |
| Mathematical modeling through graphs-Models in terms of undirected graphs, directed graphs, signed graphs and weighted graphs. Problems with engineering applications.   |  |               |
| <b>Unit –V</b>   |  | <b>09 Hrs</b> |
| <b>Variational Problem and Dynamic Programming:</b>  |  |               |
| Optimization principles and techniques, Mathematical models of variational problem and dynamic programming, Problems with engineering applications.  |  |               |

| <b>Course Outcomes: After completing the course, the students will be able to</b> |  |
|---|--|
| <b>CO1:</b>   | Explore the fundamental concepts of mathematical models arising in various fields engineering.             |
| <b>CO2:</b>   | Apply the knowledge and skills of discrete and continuous models to understand various types of analysis.  |
| <b>CO3:</b>   | Analyze the appropriate mathematical model to solve the real world problem and to optimize the solution.   |
| <b>CO4:</b>   | Distinguish the overall knowledge gained to demonstrate the problems arising in many practical situations. |

| <b>Reference Books</b> |   |
|------------------------|---|
| <b>1</b>               | Mathematical Modeling, J. N. Kapur, 1 <sup>st</sup> Edition, 1998, New Age International, New Delhi, ISBN: 81-224-0006-X.                   |
| <b>2</b>               | Case studies in mathematical modeling, D. J. G. James and J. J. Mcdonald, 1981, Stanly Thames, Cheltonham, ISBN: 0470271779, 9780470271773. |
| <b>3</b>               | Modeling with difference equations, D. N. Burghes, M. S. Borrie, Ellis Harwood, 1981, ISBN 13: 9780853122869.                               |
| <b>4</b>               | Mathematical Modeling: Models, Analysis and Applications, Sandip Banerjee, 2014, Chapman and Hall/CRC Textbook, ISBN 9781439854518.         |

#### **Continuous Internal Evaluation (CIE); Theory (100 Marks)**

CIE is executed by the way of Tests (T), Quizzes (Q,) and Experiential Learning (EL). Three tests are conducted for 50 marks each and the sum of the marks scored from three tests is reduced to 50. Minimum of three quizzes are conducted and each quiz is evaluated for 10 marks adding up to 30 marks. All quizzes are conducted online. Faculty may adopt innovative methods for conducting quizzes effectively. The number of quizzes may be more than three also. The marks component for experiential learning is 20.

**Total CIE is 50 (T) +30 (Q) +20 (EL) = 100 Marks.**

#### **Semester End Evaluation (SEE); Theory (100 Marks)**

SEE for 100 marks is executed by means of an examination. The Question paper for the course contains two parts, Part – A and Part – B. Part – A consists of objective type questions for 20 marks covering the complete syllabus. Part – B consists of five main questions, one from each unit for 16 marks adding up to 80 marks. Each main question may have sub questions. The question from Units I, IV and V have no internal choice. Units II and III have internal choice in which both questions cover entire unit having same complexity in terms of COs and Bloom's taxonomy level.

| <b>CO-PO Mapping</b> |            |            |            |            |            |            |            |            |            |             |             |             |
|----------------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|-------------|-------------|-------------|
| <b>CO/PO</b>         | <b>PO1</b> | <b>PO2</b> | <b>PO3</b> | <b>PO4</b> | <b>PO5</b> | <b>PO6</b> | <b>PO7</b> | <b>PO8</b> | <b>PO9</b> | <b>PO10</b> | <b>PO11</b> | <b>PO12</b> |
| <b>CO1</b>           | 3          | 2          | -          | 1          | -          | -          | -          | -          | -          | -           | -           | 2           |
| <b>CO2</b>           | 3          | 2          | 1          | -          | -          | -          | -          | -          | -          | -           | -           | 2           |
| <b>CO3</b>           | 2          | 3          | 2          | 2          | -          | -          | -          | -          | -          | -           | -           | 1           |
| <b>CO4</b>           | 3          | 3          | 1          | 2          | 1          | -          | -          | -          | -          | -           | -           | 3           |

**High-3: Medium-2: Low-1**